## Transforming Sinusoidal Functions

*Vertical Translation

$$
\begin{array}{ll}
y=f(x)+c & \text { Graph shifts upward } c \text { units. } \\
y=f(x)-c & \text { Graph shifts downward } c \text { units. }
\end{array}
$$

*Horizontal Translation
$y=f(x-c) \quad$ Graph shifts to the right $c$ units $y=f(x+c) \quad$ Graph shifts to the left $c$ units.
*Reflections

$$
\begin{array}{ll}
y=f(-x) & \text { Reflect graph about } y \text {-axis. } \\
y=-f(x) & \text { Reflect graph about } x \text {-axis }
\end{array}
$$

*Horizontal Stretching/ Shrinking

$$
y=f(c x) \quad \text { If } c>1 \text {, horizontal shrink (Divide each } x \text { coordinate by } c \text { ) }
$$

$$
\text { If } 0<c<1 \text {, horizontal stretch (Divide each } \mathrm{x} \text { coordinate by } \mathrm{c} \text { ) }
$$

*Vertical Stretching/Shrinking
$y=c f(x) \quad$ If $c>1$, graph is vertically stretched (Multiply each y coordinate by c) If $0<c<1$, graph is vertically shrunk (Multiply each $y$ coordinate by $c$ )

